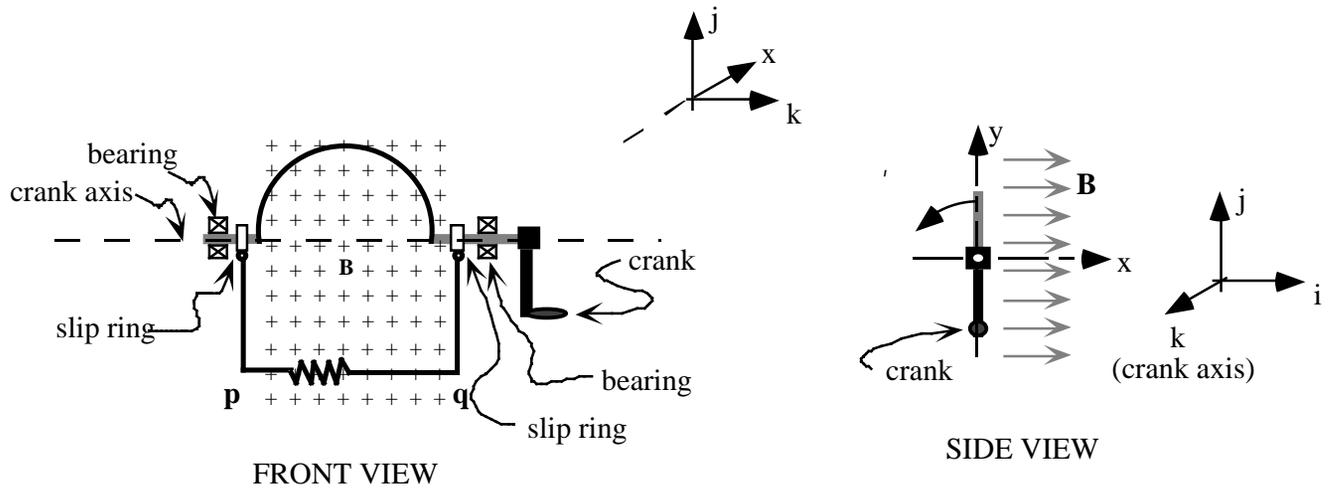


Simple AC Generator:

An electrical ac generator circuit consists of a conducting wire bent into a semi-circular shape (radius " r_0 ") and a resistor R as shown in the figure. A constant magnetic field " \mathbf{B} " (perpendicular to and inward the paper along $+x$ direction) is applied in the region. The conducting wire, bent like a semi-circular shape, is rotated by a hand crank with a constant angular velocity " ω " in the counterclockwise direction, as viewed from the crank end, and the angle " θ " is measured from the vertical position a_s shown. The area " A_0 " of the segment of the circuit below the crank axis of rotation (i.e. the z -axis) is a constant. See figures below.



Assume that at $t = 0$, the angle " θ " is zero and the circuit appears as shown in the figure on the left.

- Assuming that the angle $\theta = 0$ at $t = 0$, what is **magnetic flux** (Φ) linked to the circuit at $t = 0$? Express your answer in terms of the parameters " r_0 ", " \mathbf{B} " and " A_0 ".
- Assuming that the angle $\theta = 0$ at $t = 0$, what is **magnetic flux** (Φ) linked to the circuit at $t = \pi / \omega$? Express your answer in terms of the parameters " r_0 ", " \mathbf{B} " and " A_0 ".
- What is the "**emf**" ($\mathcal{E}(t)$) as a function of time) induced across the terminals (at the slip ring) of the conducting wire?
- Between $t=0$ and $t = \pi / \omega$, the area bounded by the circuit decreases. What is the **direction of the induced current** in the resistor during this time interval? Give reasons to substantiate your answer. What is the **magnitude** of this induced current?